

Unit 2

2.5 **Precision accuracy and uncertainty** – to be covered by Physics. Apply the concepts when carrying out calculations in this course.

- **Uncertainty in measurements**

2.6 **Significant figures** – to be covered by Physics. Apply the concepts when carrying out calculations in this course.

- **Rules for determining significant figures**
- **Rules for rounding numbers**

2.7 **Calculations involving significant figures** – to be covered by Physics. Apply the concepts when carrying out calculations in this course.

- **Rules for addition and subtraction**
- **Rules for multiplication and division**

Reading: Hebden – page 26 – 34

2.8 **Density**

Reading: Hebden – page 24 – 25

2.9 **Specific gravity**

PROBLEMS:

Significant figures

Unit conversion

Word problems

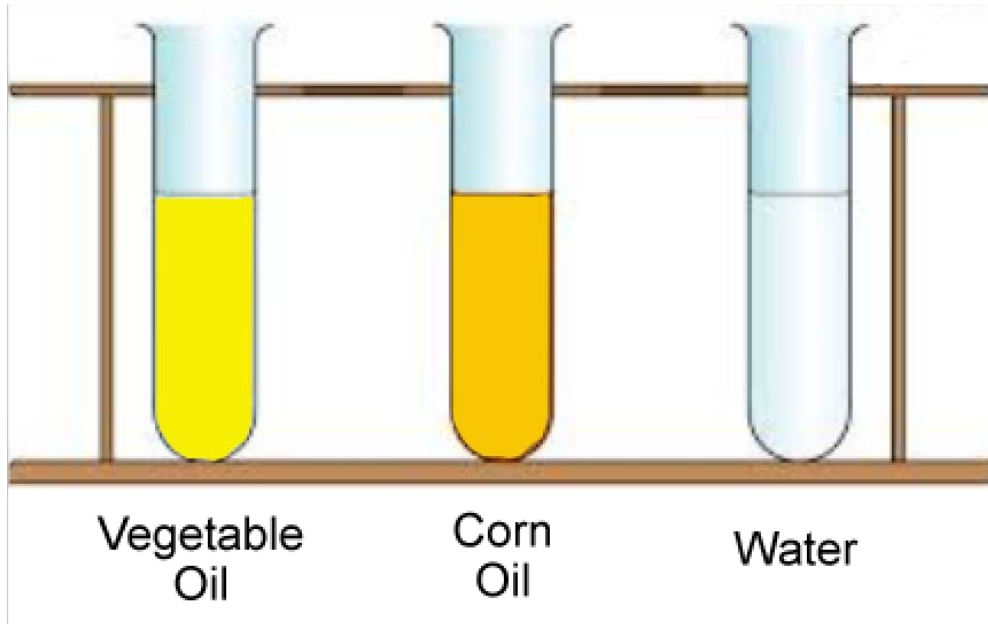
Dimensional Analysis

Unit given \times conversion factor(s) = unit sought

All about unit
cancellation

Density, D

Three liquids – *What happens when they are poured together?*



Immiscible – when liquids do not mix

Relative position is determined
by the liquid's density

Density of Vegetable Oil $< 1 \text{ g/mL}$

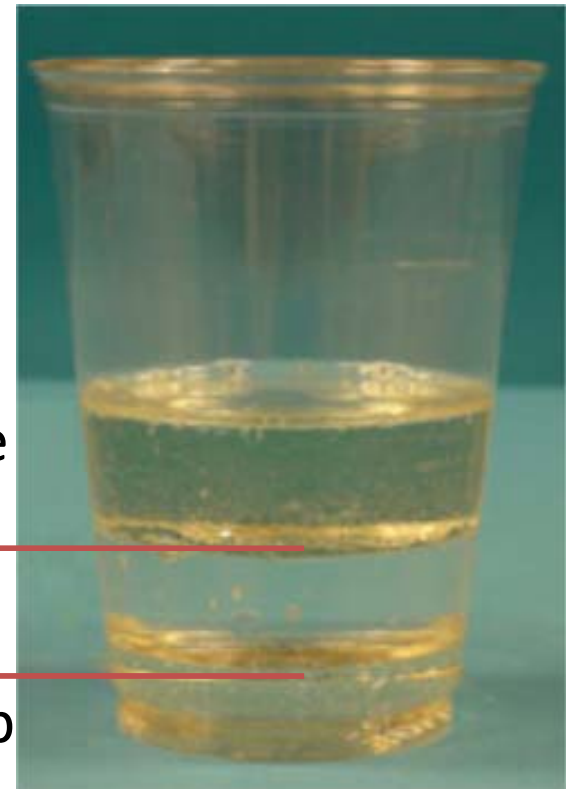
Density of water = 1 g/mL

Density of Corn Syrup $> 1 \text{ g/mL}$

Vegetable
Oil

Water

Corn Syrup



Density, D

Unit in

$$D = \frac{\text{mass}}{\text{Volume}}$$

Unit in grams, g

Unit in $\text{cm}^3, \text{mL}, \text{L}$

$\frac{\text{g}}{\text{cm}^3}, \frac{\text{g}}{\text{L}}, \frac{\text{g}}{\text{mL}}$

Express **mass** in terms of Density and volume.

$$\text{Mass} = D \cdot \text{Volume}$$

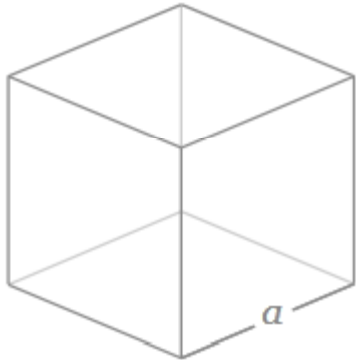
Express **volume** in terms of Density and mass.

$$\text{Volume} \cdot D = \frac{\text{mass}}{\text{Volume}} \cdot \text{Volume}$$

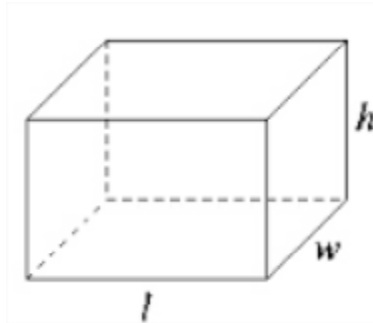
$$\frac{1}{D} \cdot \text{Volume} \cdot \cancel{D} = \text{Mass} \cdot \frac{1}{D}$$

$$\text{Volume} = \frac{\text{mass}}{D}$$

Volume



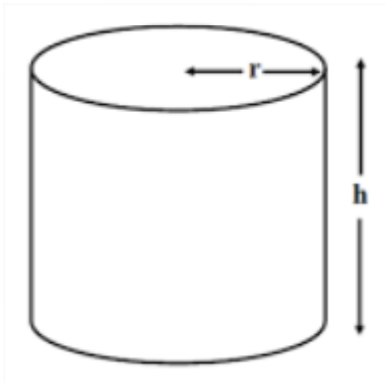
$$\text{Volume} = a^3$$



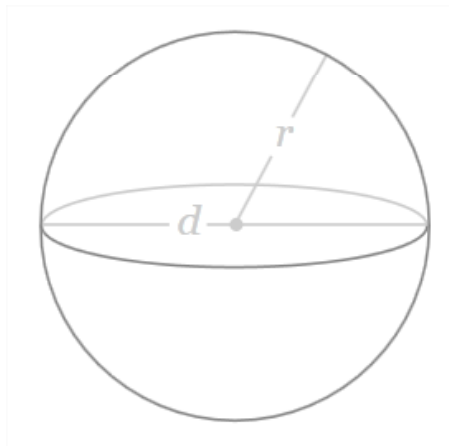
$$\text{Volume} = l \cdot w \cdot h$$



Foil: l and $w \gg h$



$$\text{Volume} = \pi r^2 h$$



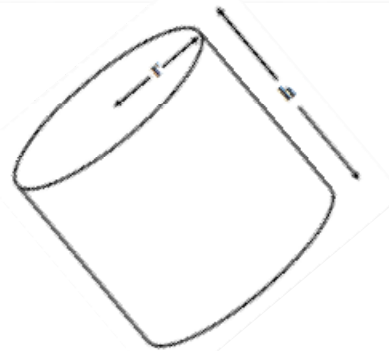
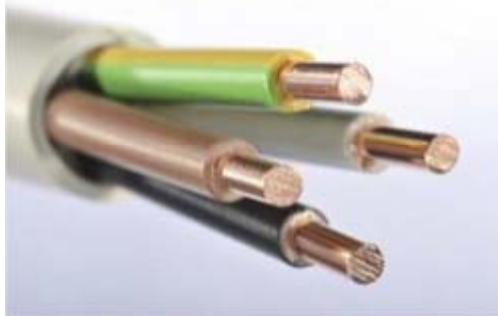
$$\text{Volume} = \frac{4}{3} \pi r^3$$



ball bearing, marble

Density Problems

The diameter of a metal wire is referred to by its wire gauge number. A 16-gauge wire has a diameter of 0.05082 inch. What length of wire, in meters, is there in a 1.00 kg of 16-gauge copper wire? The density of copper is 8.92 g/cm³.
 [Area of a circle = $\pi \cdot r^2$; 1 inch = 2.54 cm]



Wire is a cylinder, so the volume of a strand of wire can be calculated using the volume equation for a cylinder. Find h .

Density of copper = 8.92 g/cm³

$$D = \frac{\text{mass}}{\text{Volume}}$$

$$8.92 = \frac{1.00 \times 10^3}{0.0130866 \cdot h} = \frac{76414.04}{h}$$

$$h = \frac{76414.04}{8.92} = 8566.6 \text{ cm}$$

$$h = 8566.6 \text{ cm} \cdot \frac{1 \text{ m}}{100 \text{ cm}} = 85.7 \text{ m}$$

3 significant figures

$$\text{Mass} = 1.00 \text{ kg} = 1.00 \times 10^3 \text{ g}$$

Volume

$$r = \frac{1}{2} \cdot \text{diameter} = \frac{1}{2} \cdot 0.05082 \text{ inch}$$

Convert radius to centimeter, cm

Dimensional Analysis: Unit given x Conversion factor = Unit sought

$$r = \frac{1}{2} \cdot 0.05082 \text{ inch} \cdot \left(\frac{2.54 \text{ cm}}{1 \text{ in}} \right) = 0.0645414 \text{ cm}$$

$$\text{Volume} = \pi \cdot (0.0645414)^2 \cdot h = 0.0130866 h$$

$$\text{Volume} = \pi r^2 h$$

Download Density Worksheet

Scanned Lecture Notes

Road Maps:

- **Mole – Mass – Volume – Particles conversion**
- **From Percent Composition to Empirical Formula to Chemical Formula**

Worksheets:

- **Lab Report Write up Instructions**
- **Unit 2 – Density Questions Worksheet**
- Unit 3 – **Name to Chemical Formula and Chemical Formula to Name Worksheet**
- Unit 5 – **Mole Concept Worksheet**
- Unit 5 – **Salt & Sugar Worksheet**
- Unit 5 – **Solution Worksheet – Maple TA Type Questions**
- Unit 5 – **Solution Dilution Worksheet**
- Unit 5 – **Percent Composition, Empirical Formula, Chemical Formula Worksheet**

Download Density Worksheet

1. Density - volume displacement given final mass

Question:

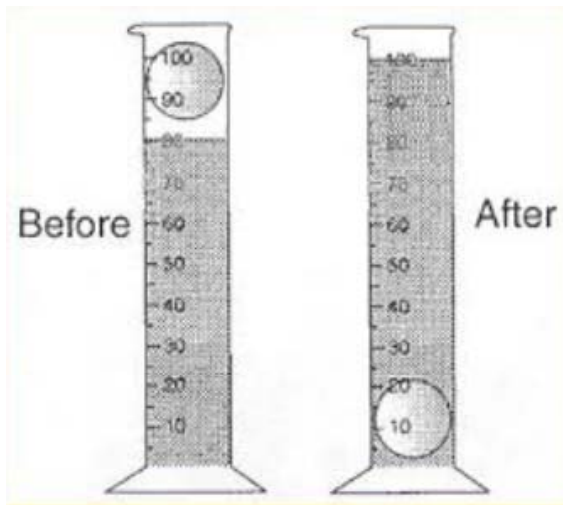
A simple way to determine the density of a solid is to immerse the solid in a known quantity of water. When a piece of metal weighing 105 g is placed in a graduated cylinder containing 203 mL of water, the final volume of water read 243 mL.

Calculate the density (in g/mL) of the metal.

  g/mL

(Answer to 2 significant figures)

$$\begin{array}{r} 243 \\ -203 \\ \hline \text{\#\# (2 sig figs)} \end{array}$$



$$D = \frac{\text{mass}}{\text{Volume}}$$

Download Density Worksheet

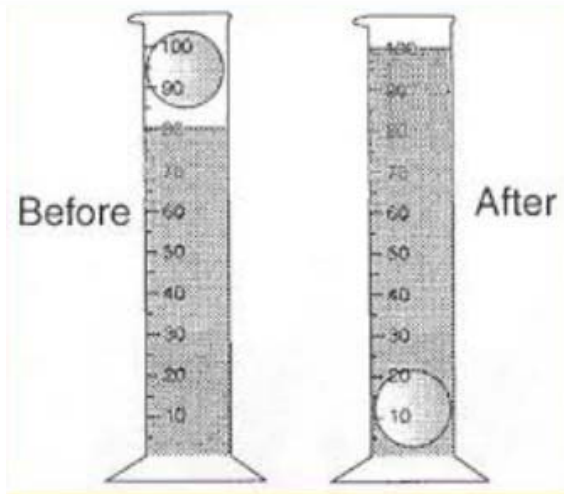
2. Density - volume displacement

A simple way to determine the density of a solid is to immerse the solid in a known quantity of water. A graduated cylinder containing 27.97 mL of water initially weighs 72.7 g. When an irregular shaped object is placed in the graduated cylinder, the final mass rises to 119 g and the volume of water rises to 35.27 mL.

Calculate the density (in g/mL) of the object.

  g/mL

(Answer to 2 significant figures)



$$D = \frac{\text{mass}}{\text{Volume}}$$

Download Density Worksheet

3. Density - volume of object is $(l)(w)(h)$

The following measurements of a metal bar were made by a student.

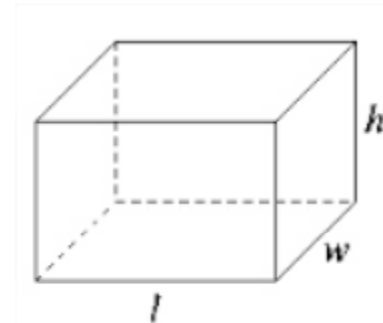
- o length = 5.10 cm
- o width = 9.10 cm
- o height = 4.10 mm Convert to centimeter first

The mass of the bar is 45 grams.

Calculate the density (g/cm^3) of the material.

  g/cm^3

(Answer to 2 significant figures)



$$\text{Volume} = l \cdot w \cdot h$$

Download Density Worksheet

4. Density - of a flask (filling with water) - given the density of water


A simple way to determine the volume of a flask is to weigh the flask when it is dry and weigh it again when it is filled with water.

The weight of the dry flask = 34.00 g

The weight of the filled flask = 115.4 g

Difference is the mass of the water

Given that the density of water is 0.996 g/mL, calculate the volume of the flask in liters.

  liter

(Answer to 3 significant figures)

$$D = \frac{\text{mass}}{\text{Volume}} \quad \rightarrow \quad \text{Volume} = \frac{\text{mass}}{D}$$

Download Density Worksheet

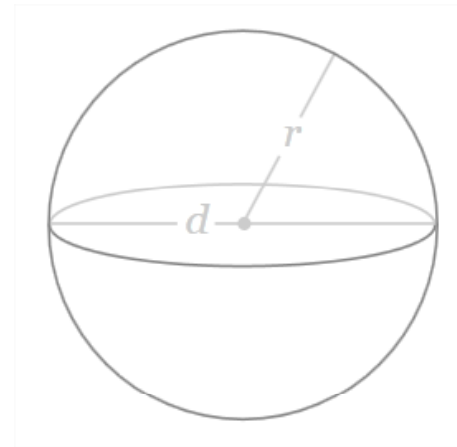
6. Density - ball bearing

Convert to centimeter first

A steel ball-bearing with a circumference of 27.5 mm weighs 5.11 g. What is the density of the steel in g/cm^3 ?
Given,

- Volume of a sphere = $(\frac{4}{3})(\pi)(r^3)$, where $\pi=3.14$.
- Circumference of a circle = $2 \pi r$

- 1.45E3 g/cm^3
- 14.5 g/cm^3
- 1.45 g/cm^3
- 0.145 g/cm^3



$$\text{Volume} = \frac{4}{3} \pi r^3$$

Steps:

1. Solve for the radius, r from the circumference.
2. Use r and solve for the volume of the ball-bearing.
3. Calculate density.

$$D = \frac{\text{mass}}{\text{Volume}}$$

Specific Gravity

Specific gravity of a substance a comparison of the density of a substance relative to a standard value. Scientists express specific gravity of liquids and solids using water at 4°C as the standard.

$$\text{specific gravity} = \frac{\text{density of substance}}{\text{density of water at } 4^{\circ}\text{C}}$$

Specific Gravity has no unit!!

In calculating the specific gravity of a substance, the density of the substance and the density of water are expressed in the same units. This leaves specific gravity unitless.

The density of water at 4°C is 1.00 g/mL. Therefore, the density of solids or liquids expressed as g/mL is numerically equal to their specific gravities.

The notation of expressing specific gravity is given below.

$$\text{specific gravity of hexane} = 0.6603 \begin{matrix} \textcircled{20} \\ \textcircled{4} \end{matrix}$$

Temperature in °C at which the density of hexane was measured

Temperature in °C at which the density of water was measured

Density changes with temperature.

- < 1 means less dense than water
- > 1 means more dense than water